

Package ‘sysid’

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Description Provides functions for constructing mathematical models of dynamical systems from measured input-output data.

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 armax

Estimate ARMAX Models

Description

Fit an ARMAX model of the specified order given the input-output data

Usage

```
armax(x, order = c(0, 1, 1, 0), init_sys = NULL, intNoise = FALSE,
      options = optimOptions())
```

Arguments

| | |
|----------|---|
| x | an object of class idframe |
| order | Specification of the orders: the four integer components (na,nb,nc,nk) are the order of polynomial A, order of polynomial B + 1, order of the polynomial C, and the input-output delay respectively |
| init_sys | Linear polynomial model that configures the initial parameterization. Must be an ARMAX model. Overrides the order argument |
| intNoise | Logical variable indicating whether to add integrators in the noise channel (Default=FALSE) |
| options | Estimation Options, setup using optimOptions |

Details

SISO ARMAX models are of the form

$$y[k] + a_1 y[k-1] + \dots + a_{na} y[k-na] = b_{nk} u[k-nk] + \dots + b_{nk+nb} u[k-nk-nb] + c_1 e[k-1] + \dots + c_{nc} e[k-nc] + e[k]$$

The function estimates the coefficients using non-linear least squares (Levenberg-Marquardt Algorithm)

The data is expected to have no offsets or trends. They can be removed using the [detrrend](#) function.

Value

An object of class estpoly containing the following elements:

| | |
|---------------|---|
| sys | an idpoly object containing the fitted ARMAX coefficients |
| fitted.values | the predicted response |
| residuals | the residuals |
| input | the input data used |
| call | the matched call |
| stats | A list containing the following fields: vcov - the covariance matrix of the fitted coefficients sigma - the standard deviation of the innovations |
| options | Option set used for estimation. If no custom options were configured, this is a set of default options |
| termination | Termination conditions for the iterative search used for prediction error minimization: WhyStop - Reason for termination iter - Number of Iterations iter - Number of Function Evaluations |

References

Arun K. Tangirala (2015), *Principles of System Identification: Theory and Practice*, CRC Press, Boca Raton. Sections 14.4.1, 21.6.2

Examples

```
data(armaxsim)
z <- dataSlice(armaxsim,end=1533) # training set
mod_armax <- armax(z,c(1,2,1,2))
mod_armax
```

armaxsim

Data simulated from an ARMAX model

Description

This dataset contains 2555 samples simulated from the following ARMAX model:

$$y[k] = \frac{0.6q^{-2} - 0.2q^{-3}}{1 - 0.5q^{-1}}u[k] + \frac{1 - 0.3q^{-1}}{1 - 0.5q^{-1}}e[k]$$

Usage

```
armaxsim
```

Format

an idframe object with 2555 samples, one input and one output

Details

The model is simulated with a 2555 samples long full-band PRBS input. The noise variance is set to 0.1

arx

Estimate ARX Models

Description

Fit an ARX model of the specified order given the input-output data

Usage

```
arx(x, order = c(1, 1, 1), lambda = 0.1, intNoise = FALSE, fixed = NULL)
```

Arguments

| | |
|----------|--|
| x | an object of class idframe |
| order | Specification of the orders: the three integer components (na,nb,nk) are the order of polynomial A, (order of polynomial B + 1) and the input-output delay |
| lambda | Regularization parameter(Default=0.1) |
| intNoise | Logical variable indicating whether to add integrators in the noise channel (Default=FALSE) |
| fixed | list containing fixed parameters. If supplied, only NA entries will be varied. Specified as a list of two vectors, each containing the parameters of polynomials A and B respectively. |

Details

SISO ARX models are of the form

$$y[k] + a_1y[k-1] + \dots + a_nay[k-na] = b_{nk}u[k-nk] + \dots + b_{nk+nb}u[k-nk-nb] + e[k]$$

The function estimates the coefficients using linear least squares (with regularization).

The data is expected to have no offsets or trends. They can be removed using the [detrnd](#) function.

To estimate finite impulse response(FIR) models, specify the first order to be zero.

Value

An object of class estpoly containing the following elements:

| | |
|---------------|---|
| sys | an idpoly object containing the fitted ARX coefficients |
| fitted.values | the predicted response |
| residuals | the residuals |
| input | the input data used |
| call | the matched call |
| stats | A list containing the following fields: vcov - the covariance matrix of the fitted coefficients sigma - the standard deviation of the innovations df - the residual degrees of freedom |

References

Arun K. Tangirala (2015), *Principles of System Identification: Theory and Practice*, CRC Press, Boca Raton. Section 21.6.1

Lennart Ljung (1999), *System Identification: Theory for the User*, 2nd Edition, Prentice Hall, New York. Section 10.1

Examples

```
data(arxsim)
mod_arx <- arx(arxsim,c(1,2,2))
mod_arx
plot(mod_arx) # plot the predicted and actual responses
```

 arxsim

Data simulated from an ARX model

Description

This dataset contains 2555 samples simulated from the following ARX model:

$$y[k] = \frac{0.6q^{-2} - 0.2q^{-3}}{1 - 0.5q^{-1}}u[k] + \frac{1}{1 - 0.5q^{-1}}e[k]$$

Usage

arxsim

Format

an idframe object with 2555 samples, one input and one output

Details

The model is simulated with a 2555 samples long full-band PRBS input. The noise variance is set to 0.1

 bj

Estimate Box-Jenkins Models

Description

Fit a box-jenkins model of the specified order from input-output data

Usage

bj(z, order = c(1, 1, 1, 1, 0), init_sys = NULL, options = optimOptions())

Arguments

| | |
|----------|---|
| z | an idframe object containing the data |
| order | Specification of the orders: the five integer components (nb,nc,nd,nf,nk) are order of polynomial B + 1, order of the polynomial C, order of the polynomial D, order of the polynomial F, and the input-output delay respectively |
| init_sys | Linear polynomial model that configures the initial parameterization. Must be a BJ model. Overrides the order argument |
| options | Estimation Options, setup using optimOptions |

Details

SISO BJ models are of the form

$$y[k] = \frac{B(q^{-1})}{F(q^{-1})}u[k - nk] + \frac{C(q^{-1})}{D(q^{-1})}e[k]$$

The orders of Box-Jenkins model are defined as follows:

$$B(q^{-1}) = b_1 + b_2q^{-1} + \dots + b_{nb}q^{-nb+1}$$

$$C(q^{-1}) = 1 + c_1q^{-1} + \dots + c_{nc}q^{-nc}$$

$$D(q^{-1}) = 1 + d_1q^{-1} + \dots + d_{nd}q^{-nd}$$

$$F(q^{-1}) = 1 + f_1q^{-1} + \dots + f_{nf}q^{-nf}$$

The function estimates the coefficients using non-linear least squares (Levenberg-Marquardt Algorithm)

The data is expected to have no offsets or trends. They can be removed using the `detrend` function.

Value

An object of class `estpoly` containing the following elements:

| | |
|----------------------------|--|
| <code>sys</code> | an <code>idpoly</code> object containing the fitted BJ coefficients |
| <code>fitted.values</code> | the predicted response |
| <code>residuals</code> | the residuals |
| <code>input</code> | the input data used |
| <code>call</code> | the matched call |
| <code>stats</code> | A list containing the following fields: <code>vcov</code> - the covariance matrix of the fitted coefficients <code>sigma</code> - the standard deviation of the innovations |
| <code>options</code> | Option set used for estimation. If no custom options were configured, this is a set of default options |
| <code>termination</code> | Termination conditions for the iterative search used for prediction error minimization: <code>WhyStop</code> - Reason for termination <code>iter</code> - Number of Iterations <code>iter</code> - Number of Function Evaluations |

References

Arun K. Tangirala (2015), *Principles of System Identification: Theory and Practice*, CRC Press, Boca Raton. Sections 14.4.1, 17.5.2, 21.6.3

Examples

```
data(bjsim)
z <- dataSlice(bjsim,end=1500) # training set
mod_bj <- bj(z,c(2,1,1,1,2))
mod_bj
residplot(mod_bj) # residual plots
```

| | |
|-------|--|
| bjsim | <i>Data simulated from an BJ model</i> |
|-------|--|

Description

This dataset contains 2046 samples simulated from the following BJ model:

$$y[k] = \frac{0.6q^{-2} - 0.2q^{-3}}{1 - 0.5q^{-1}}u[k] + \frac{1 + 0.2q^{-1}}{1 - 0.3q^{-1}}e[k]$$

Usage

```
bjsim
```

Format

an idframe object with 2046 samples, one input and one output

Details

The model is simulated with a 2046 samples long full-band PRBS input. The noise variance is set to 0.1

| | |
|---------|--|
| compare | <i>Compare the measured output and the predicted output(s)</i> |
|---------|--|

Description

Plots the output predictions of model(s) superimposed over validation data, data, for comparison.

Usage

```
compare(data, nahead = 1, ...)
```

Arguments

| | |
|--------|--|
| data | validation data in the form of an idframe object |
| nahead | number of steps ahead at which to predict (Default:1). For infinite- step ahead predictions, supply Inf. |
| ... | models whose predictions are to be compared |

See Also

[predict.estpoly](#) for obtaining model predictions

Examples

```
data(arxsim)
mod1 <- arx(arxsim,c(1,2,2))
mod2 <- oe(arxsim,c(2,1,1))
compare(arxsim,nahead=Inf,mod1,mod2)
```

cstr

Continuous stirred tank reactor data (idframe)

Description

The Process is a model of a Continuous Stirring Tank Reactor, where the reaction is exothermic and the concentration is controlled by regulating the coolant flow.

Usage

```
cstr
```

Format

an idframe object with 7500 samples, one input and two outputs

Details

Inputs: q, Coolant Flow l/min Outputs:

Ca Concentration mol/l

T Temperature Kelvin

| | |
|----------|--|
| cstrData | <i>Continuous stirred tank reactor data (data.frame)</i> |
|----------|--|

Description

The Process is a model of a Continuous Stirring Tank Reactor, where the reaction is exothermic and the concentration is controlled by regulating the coolant flow.

Usage

cstrData

Format

an `data.frame` object with 7500 rows and three columns: `q`, `Ca` and `T`

Details

Inputs: `q`, Coolant Flow l/min Outputs:

Ca Concentration mol/l

T Temperature Kelvin

Source

ftp://ftp.esat.kuleuven.be/pub/SISTA/data/process_industry/cstr.dat.gz

| | |
|----------|---|
| cstr_mis | <i>Continuous stirred tank reactor data with missing values</i> |
|----------|---|

Description

This dataset is derived from the `cstr` dataset with few samples containing missing values, in one or all variables. It is used to demonstrate the capabilities of the `misdata` routine.

Usage

cstr_mis

Format

an `idframe` object with 7500 samples, one input and two outputs

See Also

[cstr](#), [misdata](#)

| | |
|-----------|--|
| dataSlice | <i>Subset or Resample idframe data</i> |
|-----------|--|

Description

dataSlice is a subsetting method for objects of class idframe. It extracts the subset of the object data observed between indices start and end. If a frequency is specified, the series is then re-sampled at the new frequency.

Usage

```
dataSlice(data, start = NULL, end = NULL, freq = NULL)
```

Arguments

| | |
|-------|---|
| data | an object of class idframe |
| start | the start index |
| end | the end index |
| freq | fraction of the original frequency at which the series to be sampled. |

Details

The dataSlice function extends the [window](#) function for idframe objects

Value

an idframe object

See Also

[window](#)

Examples

```
data(cstr)
cstrsub <- dataSlice(cstr,start=200,end=400) # extract between indices 200 and 400
cstrTrain <- dataSlice(cstr,end=4500) # extract upto index 4500
cstrTest <- dataSlice(cstr,start=6501) # extract from index 6501 till the end
cstr_new <- dataSlice(cstr,freq=0.5) # resample data at half the original frequency
```

detrrend*Remove offsets and linear trends*

Description

Removes offsets or trends from data

Usage

```
detrrend(x, type = 0)
```

Arguments

| | |
|------|--|
| x | an object of class <code>idframe</code> |
| type | argument indicating the type of trend to be removed (Default=0) <ul style="list-style-type: none">• type=0: Subtracts mean value from each signal• type=1: Subtracts a linear trend (least-squares fit)• type=trInfo object: Subtracts a trend specified by the object |

Details

R by default doesn't allow return of multiple objects. The `%=%` operator and `g` function in this package facilitate this behaviour. See the examples section for more information.

Value

A list containing two objects: the detrended data and the trend information

See Also

[lm](#)

Examples

```
data(cstr)
datatrain <- dataSlice(cstr,end=4500)
datatest <- dataSlice(cstr,4501)
g(Ztrain,tr) %=% detrrend(datatrain) # Remove means
g(Ztest) %=% detrrend(datatest,tr)
```

| | |
|---------|------------------------------------|
| estpoly | <i>Estimated polynomial object</i> |
|---------|------------------------------------|

Description

Estimated discrete-time polynomial model returned from an estimation routine.

Usage

```
estpoly(sys, fitted.values, residuals, options = NULL, call, stats,
        termination = NULL, input)
```

Arguments

| | |
|---------------|---|
| sys | an idpoly object containing the estimated polynomial coefficients |
| fitted.values | 1-step ahead predictions on the training dataset |
| residuals | 1-step ahead prediction errors |
| options | optimization specification ser used (applicable for non-linear least squares) |
| call | the matched call |
| stats | a list containing estimation statistics |
| termination | termination criteria for optimization |
| input | input signal of the training data-set |

Details

Do not use estpoly for directly specifying an input-output polynomial model. [idpoly](#) is to be used instead

| | |
|------|---|
| etfe | <i>Estimate empirical transfer function</i> |
|------|---|

Description

Estimates the emperical transfer function from the data by taking the ratio of the fourier transforms of the output and the input variables

Usage

```
etfe(data, n = 128)
```

Arguments

| | |
|------|----------------------------------|
| data | an object of class idframe |
| n | frequency spacing (Default: 128) |

Value

an idfrd object containing the estimated frequency response

References

Arun K. Tangirala (2015), *Principles of System Identification: Theory and Practice*, CRC Press, Boca Raton. Sections 5.3 and 20.4.2

See Also

[fft](#)

Examples

```
data(arxsim)
frf <- etfe(arxsim)
```

fitch

Fit Characteristics

Description

Returns quantitative assessment of the estimated model as a list

Usage

```
fitch(x)
```

Arguments

x the estimated model

Value

A list containing the following elements

| | |
|--------|---|
| MSE | Mean Square Error measure of how well the response of the model fits the estimation data |
| FPE | Final Prediction Error |
| FitPer | Normalized root mean squared error (NRMSE) measure of how well the response of the model fits the estimation data, expressed as a percentage. |
| AIC | Raw Akaike Information Criteria (AIC) measure of model quality |
| AICc | Small sample-size corrected AIC |
| nAIC | Normalized AIC |
| BIC | Bayesian Information Criteria (BIC) |

| | |
|-----|--------------------------------|
| frd | <i>Frequency response data</i> |
|-----|--------------------------------|

Description

This dataset contains frequency response data of an unknown SISO system.

Usage

frd

Format

an idfrd object with response at 128 frequency points

| | |
|--------|---|
| getcov | <i>Parameter covariance of the identified model</i> |
|--------|---|

Description

Obtain the parameter covariance matrix of the linear, identified parametric model

Usage

getcov(sys)

Arguments

| | |
|-----|---------------------------------------|
| sys | a linear, identified parametric model |
|-----|---------------------------------------|

| | |
|---------|--|
| idframe | <i>S3 class for storing input-output data.</i> |
|---------|--|

Description

idframe is an S3 class for storing and manipulating input-output data. It supports discrete time and frequency domain data.

Usage

```
idframe(output, input = NULL, Ts = 1, start = 0, end = NULL,
        unit = c("seconds", "minutes", "hours", "days")[1])
```

Arguments

| | |
|--------|--|
| output | dataframe/matrix/vector containing the outputs |
| input | dataframe/matrix/vector containing the inputs |
| Ts | sampling interval (Default: 1) |
| start | Time of the first observation |
| end | Time of the last observation Optional Argument |
| unit | Time unit (Default: "seconds") |

Value

an idframe object

See Also

[plot.idframe](#), the plot method for idframe objects

Examples

```
dataMatrix <- matrix(rnorm(1000),ncol=5)
data <- idframe(output=dataMatrix[,3:5],input=dataMatrix[,1:2],Ts=1)
```

| | |
|-------|---|
| idfrd | <i>S3 class constructor for storing frequency response data</i> |
|-------|---|

Description

S3 class constructor for storing frequency response data

Usage

```
idfrd(respData, freq, Ts, spec = NULL, covData = NULL, noiseCov = NULL)
```

Arguments

| | |
|----------|---|
| respData | frequency response data. For SISO systems, supply a vector of frequency response values. For MIMO systems with N_y outputs and N_u inputs, supply an array of size $c(N_y, N_u, N_w)$. |
| freq | frequency points of the response |
| Ts | sampling time of data |
| spec | power spectra and cross spectra of the system output disturbances (noise). Supply an array of size (N_y, N_y, N_w) |
| covData | response data covariance matrices. Supply an array of size $(N_y, N_u, N_w, 2, 2)$. $covData[ky, ku, kw, ,]$ is the covariance matrix of $respData[ky, ku, kw]$ |
| noiseCov | power spectra variance. Supply an array of size (N_y, N_y, N_w) |

Value

an idfrd object

See Also

[plot.idfrd](#) for generating bode plots, [spa](#) and [etfe](#) for estimating the frequency response given input/output data

| | |
|---------|---|
| idinput | <i>function to generate input singals (rgs/rbs/prbs/sine)</i> |
|---------|---|

Description

idinput is a function for generating input signals (rgs/rbs/prbs/sine) for identification purposes

Usage

```
idinput(n, type = "rgs", band = c(0, 1), levels = c(-1, 1))
```

Arguments

| | |
|--------|---|
| n | integer length of the input signal to be generated |
| type | the type of input signal to be generated. 'rgs' - generates random gaussian signal 'rbs' - generates random binary signal 'prbs' - generates pseudorandom binary signal 'sine' - generates a signal that is a sum of sinusoids Default value is type='rgs' |
| band | determines the frequency content of the signal. For type='rbs'/'sine', band = [wlow,whigh] which specifies the lower and the upper bound of the passband frequencies(expressed as fractions of Nyquist frequency). Default is c(0,1) For type='prbs', band=[0,B] where B is such that the signal is constant over 1/B (clock period). Default is c(0,1) |
| levels | row vector defining the input level. It is of the form levels=c(minu, maxu) For 'rbs','prbs', 'sine', the generated signal always between minu and maxu. For 'rgs', minu=mean value of signal minus one standard deviation and maxu=mean value of signal plus one standard deviation Default value is levels=c(-1,1) |

idpoly

*Polynomial model with identifiable parameters***Description**

Creates a polynomial model with identifiable coefficients

Usage

```
idpoly(A = 1, B = 1, C = 1, D = 1, F1 = 1, ioDelay = 0, Ts = 1,
       noiseVar = 1, intNoise = F, unit = c("seconds", "minutes", "hours",
       "days")[1])
```

Arguments

| | |
|----------|--|
| A | autoregressive coefficients |
| B, F1 | coefficients of the numerator and denominator respectively of the deterministic model between the input and output |
| C, D | coefficients of the numerator and denominator respectively of the stochastic model |
| ioDelay | the delay in the input-output channel |
| Ts | sampling interval |
| noiseVar | variance of the white noise source (Default=1) |
| intNoise | Logical variable indicating presence or absence of integrator in the noise channel (Default=FALSE) |
| unit | time unit (Default="seconds") |

Details

Discrete-time polynomials are of the form

$$A(q^{-1})y[k] = \frac{B(q^{-1})}{F1(q^{-1})}u[k] + \frac{C(q^{-1})}{D(q^{-1})}e[k]$$

Examples

```
# define output-error model
mod_oe <- idpoly(B=c(0.6,-0.2),F1=c(1,-0.5),ioDelay = 2,Ts=0.1,
noiseVar = 0.1)

# define box-jenkins model with unit variance
B <- c(0.6,-0.2)
C <- c(1,-0.3)
D <- c(1,1.5,0.7)
F1 <- c(1,-0.5)
mod_bj <- idpoly(1,B,C,D,F1,ioDelay=1)
```

| | |
|------------|---|
| impulseest | <i>Estimate Impulse Response Coefficients</i> |
|------------|---|

Description

impulseest is used to estimate impulse response coefficients from the data

Usage

```
impulseest(x, M = 30, K = NULL, regul = F, lambda = 1)
```

Arguments

| | |
|--------|--|
| x | an object of class idframe |
| M | Order of the FIR Model (Default:30) |
| K | Transport delay in the estimated impulse response (Default:NULL) |
| regul | Parameter indicating whether regularization should be used. (Default:FALSE) |
| lambda | The value of the regularization parameter. Valid only if regul=TRUE. (Default:1) |

Details

The IR Coefficients are estimated using linear least squares. Future Versions will provide support for multivariate data.

References

Arun K. Tangirala (2015), *Principles of System Identification: Theory and Practice*, CRC Press, Boca Raton. Sections 17.4.11 and 20.2

See Also

[step](#)

Examples

```
uk <- rnorm(1000,1)
yk <- filter(uk,c(0.9,-0.4),method="recursive") + rnorm(1000,1)
data <- idframe(output=data.frame(yk),input=data.frame(uk))
fit <- impulseest(data)
impulseplot(fit)
```

`impulseplot`*Impulse Response Plots*

Description

Plots the estimated IR coefficients along with the significance limits at each lag.

Usage

```
impulseplot(model, sd = 2)
```

Arguments

| | |
|--------------------|--|
| <code>model</code> | an object of class <code>impulseeest</code> |
| <code>sd</code> | standard deviation of the confidence region (Default: 2) |

See Also

[impulseeest,step](#)

`inputData`*Output or Input-data*

Description

Extract output-data or input-data in `idframe` objects

Usage

```
inputData(x, series)
```

Arguments

| | |
|---------------------|-----------------------------|
| <code>x</code> | <code>idframe</code> object |
| <code>series</code> | the indices to extract |

| | |
|--------------|-------------------------------------|
| inputNames<- | <i>Extract or set series' names</i> |
|--------------|-------------------------------------|

Description

Extract or set names of series in input or output

Usage

```
inputNames(x) <- value
```

Arguments

| | |
|-------|-------------------|
| x | idframe object |
| value | vector of strings |

| | |
|----|--|
| iv | <i>ARX model estimation using instrumental variable method</i> |
|----|--|

Description

Estimates an ARX model of the specified order from input-output data using the instrument variable method. If arbitrary instruments are not supplied by the user, the instruments are generated using the arx routine

Usage

```
iv(z, order = c(0, 1, 0), x = NULL)
```

Arguments

| | |
|-------|--|
| z | an idframe object containing the data |
| order | Specification of the orders: the three integer components (na,nb,nk) are the order of polynomial A, (order of polynomial B + 1) and the input-output delay |
| x | instrument variable matrix. x must be of the same size as the output data. (Default: NULL) |

Value

An object of class `estpoly` containing the following elements:

| | |
|----------------------------|--|
| <code>sys</code> | an <code>idpoly</code> object containing the fitted ARX coefficients |
| <code>fitted.values</code> | the predicted response |
| <code>residuals</code> | the residuals |
| <code>input</code> | the input data used |
| <code>call</code> | the matched call |
| <code>stats</code> | A list containing the following fields: <code>vcov</code> - the covariance matrix of the fitted coefficients <code>sigma</code> - the standard deviation of the innovations <code>df</code> - the residual degrees of freedom |

References

Arun K. Tangirala (2015), *Principles of System Identification: Theory and Practice*, CRC Press, Boca Raton. Sections 21.7.1, 21.7.2

Lennart Ljung (1999), *System Identification: Theory for the User*, 2nd Edition, Prentice Hall, New York. Section 7.6

See Also

[arx](#), [iv4](#)

Examples

```
data(arxsim)
mod_iv <- iv(arxsim,c(2,1,1))
```

| | |
|-----|---|
| iv4 | <i>ARX model estimation using four-stage instrumental variable method</i> |
|-----|---|

Description

Estimates an ARX model of the specified order from input-output data using the instrument variable method. The estimation algorithm is insensitive to the color of the noise term.

Usage

```
iv4(z, order = c(0, 1, 0))
```

Arguments

| | |
|--------------------|---|
| <code>z</code> | an <code>idframe</code> object containing the data |
| <code>order</code> | Specification of the orders: the three integer components (<code>na,nb,nk</code>) are the order of polynomial A, (order of polynomial B + 1) and the input-output delay |

Details

Estimation is performed in 4 stages. The first stage uses the `arx` function. The resulting model generates the instruments for a second-stage IV estimate. The residuals obtained from this model are modeled using a sufficiently high-order AR model. At the fourth stage, the input-output data is filtered through this AR model and then subjected to the IV function with the same instrument filters as in the second stage.

Value

An object of class `estpoly` containing the following elements:

| | |
|----------------------------|--|
| <code>sys</code> | an <code>idpoly</code> object containing the fitted ARX coefficients |
| <code>fitted.values</code> | the predicted response |
| <code>residuals</code> | the residuals |
| <code>input</code> | the input data used |
| <code>call</code> | the matched call |
| <code>stats</code> | A list containing the following fields: <code>vcov</code> - the covariance matrix of the fitted coefficients <code>sigma</code> - the standard deviation of the innovations <code>df</code> - the residual degrees of freedom |

References

Lennart Ljung (1999), *System Identification: Theory for the User*, 2nd Edition, Prentice Hall, New York. Section 15.3

See Also

[arx](#), [iv4](#)

Examples

```
mod_dgp <- idpoly(A=c(1,-0.5),B=c(0.6,-.2),C=c(1,0.6),ioDelay = 2,noiseVar = 0.1)
u <- idinput(400,"prbs")
y <- sim(mod_dgp,u,addNoise=TRUE)
z <- idframe(y,u)
mod_iv4 <- iv4(z,c(1,2,2))
```

| | |
|---------|--|
| misdata | <i>Replace Missing Data by Interpolation</i> |
|---------|--|

Description

Function for replacing missing values with interpolated ones. This is an extension of the `na.approx` function from the `zoo` package. The missing data is indicated using the value `NA`.

Usage

```
misdata(data)
```

Arguments

`data` an object of class `idframe`

Value

`data` (an `idframe` object) with missing data replaced.

See Also

[na.approx](#)

Examples

```
data(cstr_mis)
summary(cstr_mis) # finding out the number of NAs
cstr <- misdata(cstr_mis)
```

| | |
|--------------|--|
| nInputSeries | <i>Number of series in input or output</i> |
|--------------|--|

Description

Number of series in input or output in a `idframe` object

Usage

```
nInputSeries(data)
```

Arguments

`data` `idframe` object

 oe *Estimate Output-Error Models*

Description

Fit an output-error model of the specified order given the input-output data

Usage

```
oe(x, order = c(1, 1, 0), init_sys = NULL, options = optimOptions())
```

Arguments

| | |
|----------|---|
| x | an object of class <code>idframe</code> |
| order | Specification of the orders: the four integer components (nb,nf,nk) are order of polynomial B + 1, order of the polynomial F, and the input-output delay respectively |
| init_sys | Linear polynomial model that configures the initial parameterization. Must be an OE model. Overrides the order argument |
| options | Estimation Options, setup using optimOptions |

Details

SISO OE models are of the form

$$y[k] + f_1 y[k-1] + \dots + f_n y[k-n] = b_{nk} u[k-nk] + \dots + b_{nk+nb} u[k-nk-nb] + f_1 e[k-1] + \dots + f_n e[k-n] + e[k]$$

The function estimates the coefficients using non-linear least squares (Levenberg-Marquardt Algorithm)

The data is expected to have no offsets or trends. They can be removed using the [detrrend](#) function.

Value

An object of class `estpoly` containing the following elements:

| | |
|---------------|---|
| sys | an <code>idpoly</code> object containing the fitted OE coefficients |
| fitted.values | the predicted response |
| residuals | the residuals |
| input | the input data used |
| call | the matched call |
| stats | A list containing the following fields: vcov - the covariance matrix of the fitted coefficients sigma - the standard deviation of the innovations |
| options | Option set used for estimation. If no custom options were configured, this is a set of default options |

termination Termination conditions for the iterative search used for prediction error minimization: WhyStop - Reason for termination
 iter - Number of Iterations
 iter - Number of Function Evaluations

References

Arun K. Tangirala (2015), *Principles of System Identification: Theory and Practice*, CRC Press, Boca Raton. Sections 14.4.1, 17.5.2, 21.6.3

Examples

```

data(oesim)
z <- dataSlice(oesim,end=1533) # training set
mod_oe <- oe(z,c(2,1,2))
mod_oe
plot(mod_oe) # plot the predicted and actual responses

```

oesim

Data simulated from an OE model

Description

This dataset contains 2555 samples simulated from the following OE model:

$$y[k] = \frac{0.6q^{-2} - 0.2q^{-3}}{1 - 0.5q^{-1}}u[k] + e[k]$$

Usage

oesim

Format

an idframe object with 2555 samples, one input and one output

Details

The model is simulated with a 2555 samples long full-band PRBS input. The noise variance is set to 0.1

| | |
|--------------|------------------------------------|
| optimOptions | <i>Create optimization options</i> |
|--------------|------------------------------------|

Description

Specify optimization options that are to be passed to the numerical estimation routines

Usage

```
optimOptions(tol = 0.01, maxIter = 20, LMinit = 0.01, LMstep = 2,
  display = c("off", "on")[1])
```

Arguments

| | |
|---------|---|
| tol | Minimum 2-norm of the gradient (Default: 1e-2) |
| maxIter | Maximum number of iterations to be performed |
| LMinit | Starting value of search-direction length in the Levenberg-Marquardt method (Default: 0.01) |
| LMstep | Size of the Levenberg-Marquardt step (Default: 2) |
| display | Argument whether to display iteration details or not (Default: "off") |

| | |
|--------------|---------------------------------|
| plot.idframe | <i>Plotting idframe objects</i> |
|--------------|---------------------------------|

Description

Plotting method for objects inheriting from class idframe

Usage

```
## S3 method for class 'idframe'
plot(x, col = "steelblue", lwd = 1, main = NULL,
  size = 12, ...)
```

Arguments

| | |
|------|--|
| x | an idframe object |
| col | line color, to be passed to plot.(Default="steelblue") |
| lwd | line width, in millimeters(Default=1) |
| main | the plot title. (Default = NULL) |
| size | text size (Default = 12) |
| ... | additional arguments |

Examples

```
data(cstr)
plot(cstr,col="blue")
```

plot.idfrd

Plotting idfrd objects

Description

Generates the bode plot of the given frequency response data. It uses the ggplot2 plotting engine

Usage

```
## S3 method for class 'idfrd'
plot(x, col = "steelblue", lwd = 1, ...)
```

Arguments

| | |
|-----|--|
| x | An object of class idframe |
| col | a specification for the line colour (Default : " steelblue") |
| lwd | the line width, a positive number, defaulting to 1 |
| ... | additional arguments |

See Also

[ggplot](#)

Examples

```
data(frd)
plot(frd)
```

predict.estpoly

Predictions of identified model

Description

Predicts the output of an identified model (estpoly) object K steps ahead.

Usage

```
## S3 method for class 'estpoly'
predict(object, newdata = NULL, nahead = 1, ...)
```

Arguments

| | |
|---------|---|
| object | estpoly object containing the identified model |
| newdata | optional dataset to be used for predictions. If not supplied, predictions are made on the training set. |
| nahead | number of steps ahead at which to predict (Default:1). For infinite- step ahead predictions or pure simulation, supply Inf. |
| ... | other arguments |

Value

Time-series containing the predictions

References

Arun K. Tangirala (2015), *Principles of System Identification: Theory and Practice*, CRC Press, Boca Raton. Chapter 18

Examples

```
data(arxsim)
mod1 <- oe(arxsim,c(2,1,1))
Yhat <- predict(mod1,arxsim) # 1-step ahead predictions
Yhat_2 <- predict(mod1,arxsim,nahead=2) # 2-step ahead predictions
Yhat_inf <- predict(mod1,arxsim,nahead=Inf) # Infinite-step ahead predictions
```

 rarx

Estimate parameters of ARX recursively

Description

Estimates the parameters of a single-output ARX model of the specified order from data using the recursive weighted least-squares algorithm.

Usage

```
rarx(x, order = c(1, 1, 1), lambda = 0.95)
```

Arguments

| | |
|--------|--|
| x | an object of class idframe |
| order | Specification of the orders: the three integer components (na,nb,nk) are the order of polynomial A, (order of polynomial B + 1) and the input-output delay |
| lambda | Forgetting factor(Default=0.95) |

Value

A list containing the following objects

theta Estimated parameters of the model. The k^{th} row contains the parameters associated with the k^{th} sample. Each row in theta has the following format:

theta[i,:]=[a1,a2,...,ana,b1,...,bnb]

yhat Predicted value of the output, according to the current model - parameters based on all past data

References

Arun K. Tangirala (2015), *Principles of System Identification: Theory and Practice*, CRC Press, Boca Raton. Section 25.1.3

Lennart Ljung (1999), *System Identification: Theory for the User*, 2nd Edition, Prentice Hall, New York. Section 11.2

Examples

```
Gp1 <- idpoly(c(1,-0.9,0.2),2,ioDelay=2,noiseVar = 0.1)
Gp2 <- idpoly(c(1,-1.2,0.35),2.5,ioDelay=2,noiseVar = 0.1)
uk = idinput(2044,'prbs',c(0,1/4)); N = length(uk);
N1 = round(0.35*N); N2 = round(0.4*N); N3 = N-N1-N2;
yk1 <- sim(Gp1,uk[1:N1],addNoise = TRUE)
yk2 <- sim(Gp2,uk[N1+1:N2],addNoise = TRUE)
yk3 <- sim(Gp1,uk[N1+N2+1:N3],addNoise = TRUE)
yk <- c(yk1,yk2,yk3)
z <- idframe(yk,uk,1)
g(theta,yhat) %=% rarx(z,c(2,1,2))
```

read.idframe

Data input into a idframe object

Description

Read the contents of a data.frame/matrix into a idframe object.

Usage

```
read.idframe(data, ninputs = NULL, Ts = 1, unit = c("seconds", "minutes",
"hours", "days")[1])
```

Arguments

| | |
|---------|---|
| data | a data.frame object |
| ninputs | the number of input columns. (Default: 0) |
| Ts | sampling interval (Default: 1) |
| unit | Time Unit (Default: "seconds") |

Value

an idframe object

Examples

```
data(cstrData)
data <- read.idframe(cstrData,ninputs=1,Ts= 1,unit="minutes")
```

read.table.idframe *Read the contents of a table-formatted file*

Description

Read the contents of an file in table format into a idframe object.

Usage

```
read.table.idframe(file, header = TRUE, sep = ",", ninputs = 0, Ts = 1,
  unit = c("seconds", "minutes", "hours", "days")[1], ...)
```

Arguments

| | |
|---------|---|
| file | the path to the file to read |
| header | a logical value indicating whether the first row corresponding to the first element of the rowIndex vector contains the names of the variables. (Default: TRUE) |
| sep | the field separator character. Values on each line of the file are separated by this character. (Default: ",") |
| ninputs | the number of input columns. (Default: 0) |
| Ts | sampling interval (Default: 1) |
| unit | Time Unit (Default: "seconds") |
| ... | additional arguments to be passed to the read.table function |

Details

The `read.table.idframe` function uses the [read.table](#) function, provided by the **utils** package, to read data from a table-formatted file and then calls the [read.idframe](#) function to read the data into a idframe object

Value

an idframe object

See Also

[read.table](#)

Examples

```

dataMatrix <- data.frame(matrix(rnorm(1000), ncol=5))
colnames(dataMatrix) <- c("u1", "u2", "y1", "y2", "y3")
write.csv(dataMatrix, file="test.csv", row.names=FALSE)

data <- read.table.idframe("test.csv", ninputs=2, unit="minutes")

```

| | |
|-----------|--------------------------------------|
| residplot | <i>Plot residual characteristics</i> |
|-----------|--------------------------------------|

Description

Computes the 1-step ahead prediction errors (residuals) for an estimated polynomial model, and plots auto-correlation of the residuals and the cross-correlation of the residuals with the input signals.

Usage

```
residplot(model, newdata = NULL)
```

Arguments

| | |
|---------|---|
| model | estimated polynomial model |
| newdata | an optional dataset on which predictions are to be computed. If not supplied, predictions are computed on the training dataset. |

| | |
|-----|--|
| sim | <i>Simulate response of dynamic system</i> |
|-----|--|

Description

Simulate the response of a system to a given input

Usage

```
sim(model, input, addNoise = F, innov = NULL, seed = NULL)
```


Arguments

| | |
|----------|--|
| model | the linear system to simulate |
| input | a vector/matrix containing the input |
| addNoise | logical variable indicating whether to add noise to the response model. (Default: FALSE) |
| innov | an optional times series of innovations. If not supplied (specified as NULL), gaussian white noise is generated, with the variance specified in the model (Property: noiseVar) |
| seed | integer indicating the seed value of the random number generator. Useful for reproducibility purposes. |

Details

The routine is currently built only for SISO systems. Future versions will include support for MIMO systems.

Value

a vector containing the simulated output

Examples

```
# ARX Model
u <- idinput(300,"rgs")
model <- idpoly(A=c(1,-1.5,0.7),B=c(0.8,-0.25),ioDelay=1,
noiseVar=0.1)
y <- sim(model,u,addNoise=TRUE)
```

spa

Estimate frequency response

Description

Estimates frequency response and noise spectrum from data with fixed resolution using spectral analysis

Usage

```
spa(x, winsize = NULL, freq = NULL)
```

Arguments

| | |
|---------|---|
| x | an idframe object |
| winsize | lag size of the Hanning window (Default: $\min(\text{length}(x)/10, 30)$) |
| freq | frequency points at which the response is evaluated (Default: $\text{seq}(1, 128)/128*\pi/Ts$) |

Value

an idfrd object containing the estimated frequency response and the noise spectrum

References

Arun K. Tangirala (2015), *Principles of System Identification: Theory and Practice*, CRC Press, Boca Raton. Sections 16.5 and 20.4

Examples

```
data(arxsim)
frf <- spa(arxsim)
```

step

Step Response Plots

Description

Plots the step response of a system, given the IR model

Usage

```
step(model)
```

Arguments

model an object of class impulseest

See Also

[impulseest](#)

Examples

```
uk <- rnorm(1000,1)
yk <- filter (uk,c(0.9,-0.4),method="recursive") + rnorm(1000,1)
data <- idframe(output=data.frame(yk),input=data.frame(uk))
fit <- impulseest(data)
step(fit)
```

| | |
|------|--|
| time | <i>Sampling times of IO data</i> time creates the vector of times at which data was sampled. frequency returns the number of damples per unit time and deltat the time-interval between observations |
|------|--|

Description

Sampling times of IO data

time creates the vector of times at which data was sampled. frequency returns the number of damples per unit time and deltat the time-interval between observations

Usage

```
time(x)
```

Arguments

| | |
|---|--|
| x | a idframe object, or a univariate or multivariate time-series, or a vector or matrix |
|---|--|

| | |
|-----|-------------------------------------|
| %=% | <i>Multiple assignment operator</i> |
|-----|-------------------------------------|

Description

Assign multiple variables from a list or function return object

Usage

```
l %=% r
```

Arguments

| | |
|---|------------------------------------|
| l | the variables to be assigned |
| r | the list or function-return object |

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